





Bonding in Boron Clusters | Very Important Paper |

B₃₃⁻ and B₃₄⁻: Aromatic Planar Boron Clusters with a Hexagonal Vacancy

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Abstract: Systematic experimental and theoretical studies have shown that anionic boron clusters (B_n^-) possess planar or quasi-planar (2D) structures in a wide range of cluster size. The 2D structures consist of B_3 triangles often decorated with tetragonal and pentagonal defects. As *n* increases, hexagonal vacancies appear to be a key structural feature, which underlies the stability of borophenes. The correlation of the defects with cluster size is important to understand the stability and structural evolution of boron clusters. Here we report an investigation of the structures and chemical bonding of B_{33}^- and B_{34}^- using photoelectron spectroscopy (PES) and density functional

Introduction

Boron clusters are interesting because of the prospects to discover boron analogues of the celebrated carbon fullerenes, graphene, and nanotubes.^[1-3] Early theoretical studies suggested that the B₁₂ icosahedral unit prevalent in bulk boron^[4] is not stable as isolated clusters relative to planar or quasiplanar (2D) structures.^[5-13] Over the past decade, joint experimental and theoretical investigations have uncovered a rich 2D world for size-selected boron clusters.^[14-42] Ion mobility measurements in combination with density functional theory (DFT) calculations suggested that cationic B_n^+ clusters have 2D structures up to n = 16.^[14] Theoretical calculations showed that the critical size of 2D to 3D tubular transition for neutral boron clusters occurs at B₂₀,^[30] even though the tubular structure was not observed in an infrared spectroscopy study.[17,43] The most extensive experimental studies have been on size-selected negatively charged boron clusters (B_n^{-}) using photoelectron spectroscopy (PES).^[17] Joint PES and theoretical investigations have

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theory (DFT) calculations. Global minimum searches reveal that the potential landscapes of B₃₃⁻ and B₃₄⁻ are dominated by 2D isomers. Comparisons between experiment and theory confirm that their global-minimum structures are both 2D with a hexagonal vacancy (C_s B₃₃⁻) and (C_1 B₃₄⁻), the latter being a chiral cluster. Bonding analyses indicate that the C_s B₃₃⁻ cluster possesses ten delocalized π bonds, analogous to those in the polycyclic aromatic hydrocarbon C₁₉H₁₁⁻. Bonding analyses on the equivalent closed-shell B₃₄²⁻ species show that its 12 delocalized π bonds consist of two separate aromatic systems: nine exterior and three interior π bonds.

shown 2D structures exist up to n = 40.^[15–42] Chemical bonding analyses revealed that 2D boron clusters are characterized by both delocalized σ and π bonding, resulting in concepts of aromaticity, antiaromaticity, and all-boron analogues of hydrocarbons.^[15–44]

The 2D B_n^- clusters elucidated by joint PES and theoretical studies are all composed of B₃ triangles often with tetragonal, pentagonal, and hexagonal vacancies as the cluster size increases. These polygonal defects or vacancies play critical roles in the stability of the 2D boron clusters.^[26-42] Interestingly, the presence of these defects results in structural fluxionality in the cluster plane,^[16,17,29] which have inspired proposals of molecular Wankel motors and other dynamic effects.^[45-51] The first 2D boron cluster discovered to contain a hexagonal vacancy was B_{36} , which was observed to have pseudo- C_{6v} symmetry.^[41] Neutral B_{36} has perfect C_{6v} symmetry and can serve as a basic building unit for 2D boron monolayers, for which a name "borophene" was coined.^[41] The hexagonal B₃₆ cluster provided the first indirect experimental evidence for the viability of borophenes. The double-hexagonal vacancy observed in B₃₅⁻ makes it an even more flexible motif to construct borophenes.^[40] The global minimum of B_{30}^{-} was found to be a 2D chiral structure with a hexagonal vacancy.^[39] The smallest boron cluster (B_{26} ⁻) with a hexagonal vacancy was reported recently,^[35] whereas B₃₇⁻ and B₃₈⁻ was found very recently to contain a double-hexagonal vacancy similar to that in B₃₅^{-.[42]} Another major breakthrough in size-selected boron clusters is the discovery of the first all-boron fullerenes, $D_{2d} B_{40}^{-/0}$, named borospherenes using joint PES and theoretical studies.^[52] Even though the global minimum of B_{40}^{-} is a 2D structure with the B_{40}^{-} borospherene as a co-existing isomer, the neutral B40 borospherene is the

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overwhelming global minimum. Subsequently, B_{39}^- was found to consist of two close-lying chiral borospherenes of C_3 and C_2 symmetries.^[53] Less symmetric and seashell-like B_{28}^- and $B_{29}^$ borospherenes were also observed experimentally as low-lying isomers.^[37,38]

The size of the vacancy seems to increase with cluster size in 2D boron clusters from tetragonal to pentagonal and hexagonal. The first double-hexagonal vacancy appeared in $B_{35}^{-[40]}$ Hence, the clusters from B_{31}^{-} to B_{34}^{-} represent the size range where the cluster structure evolves from a single hexagonal vacancy to a double-hexagonal vacancy. However, these four critical clusters have not been studied heretofore. In the present work, we report an investigation on the structures and chemical bonding of B_{33}^{-} and B_{34}^{-} using PES in conjunction with global minimum searches and DFT calculations. The global minima of both B_{33}^{-} and B_{34}^{-} are identified as 2D structures with a single hexagonal vacancy, with B_{34}^{-} being chiral similar to the chiral $B_{30}^{-[39]}$

Results

Photoelectron Spectroscopy

The PES experiment was done with a magnetic bottle electron analyzer equipped with a laser-vaporization cluster source.^[17,54] The PE spectra of B_{33}^- and B_{34}^- are shown in Figure 1 and Figure 2, respectively, in comparison with simulated spectra from the respective global minimum. The observed spectral features are labeled with letters (X, A, ..., E) and the measured vertical detachment energies (VDEs) are given in Table S1.



Figure 1. The photoelectron spectrum of (a) B_{33}^- at 193 nm (6.424 eV), compared to (b) the simulated spectrum of the global minimum of B_{33}^- (I, C_s). Vertical bars in (b) denote calculated VDEs at the TD-PBE0/6-311+G(d) level.

The PE spectrum of B_{33}^{-} shown in Figure 1a is fairly congested. Six spectral bands (X, A–E) can be identified, though each may contain multiple detachment channels. The adiabatic detachment energy (ADE) for the ground state band X (VDE: 4.09 eV) was evaluated from its leading edge as 3.91 ± 0.06 eV, which also represents the electron affinity (EA) of neutral B_{33} . Band A is weaker with a VDE of 4.62 eV, beyond which the





Figure 2. The photoelectron spectrum of (a) B_{34}^- at 193 nm, compared to (b) the simulated spectrum of the global minimum of B_{34}^- . Vertical bars in (b) denote calculated VDEs at the TD-PBE0/6-311+G(d) level. The longer bars are for triplet final states and the shorter ones for singlet final states.

spectrum is nearly continuous. The labels from B to E are for the sake of discussion only.

The PE spectrum of B_{34}^- (Figure 2a) displays two separated spectral regions. In the lower binding energy region, three overlapping bands (X, A, B) are observed between 3.5 and 4.5 eV with VDEs of 3.89, 4.02, and 4.28 eV respectively. The ADE of band X, that is, the EA of neutral B_{34} , is estimated to be 3.75 ± 0.06 eV from the band onset. In the higher binding energy region beyond 4.7 eV, the spectrum is even more congested with higher relative intensities. Three bands (C, D, E) can be tentatively identified, each being expected to contain multiple detachment transitions.

Computational Results

The global minima of B_{33}^- and B_{34}^- were searched using the TGMin code.^[55,56] Candidate structures were subsequently reoptimized at the PBE0/6-311+G(d) level.^[57-59] Low-lying isomers of B_{33}^- and B_{34}^- within 1 eV are shown in Figures S1 and S2,



Figure 3. The global minimum and low-lying isomers of (a) B_{33}^- and (b) B_{34}^- . Relative energies at the PBE0/6-311+G(d) level (including ZPE corrections) are shown in eV. Note the global minimum of B_{34}^- (V and VI) are enantiomers.





respectively. The four lowest-lying structures of B_{33}^- and B_{34}^- are presented in Figure 3. All the relative energies were corrected for zero-point energies (ZPEs). Cartesian coordinates for the most stable B_{33}^- and B_{34}^- clusters are given in Table S2.

Global Minimum and Low-Lying Isomers of B₃₃⁻

The global minimum of B_{33}^{-} is 2D (I C_{sr} ¹A') with an overall diamond shape and a central hexagonal vacancy (Figure 3a). The 2D structure, consisting of eighteen peripheral and fifteen interior atoms, is quasi-planar with an out-of-plane distortion of 1.72 Å. At the PBE0/6-311+G(d) levels, isomers II, III, and IV are 0.24, 0.31, and 0.33 eV above the global minimum, respectively. Isomer II (C_1 , ¹A) is a severely distorted 2D structure with a hexagonal vacancy and a filled pentagon. Isomer III (C_{sr} ¹A') is a distorted 3D tubular-like structure with a filled pentacoordinate B site. The less distorted triple-ring tubular isomer is 1.55 eV above I (Figure S1). Isomer IV (C_2 , ¹A) consists of a buckled triangular lattice.

As shown in Figure S1, 29 isomers were found within 1 eV of the global minimum of B_{33}^{-} . Except the two 2D isomers with buckled triangular lattices and five 3D structures, the rest of the isomers all have 2D structures with pentagonal, hexagonal or heptagonal vacancies. Hence, the potential energy surface of B_{33}^{-} is dominated by 2D structures with polygonal vacancies. It is interesting to note that the isomer with a double-hexagonal vacancy is 0.90 eV higher in energy.

Global Minimum and Low-Lying Isomers of B₃₄⁻

The global minimum of B_{34}^- is also 2D with a hexagonal vacancy (isomer **V** in Figure 3b). It consists of eighteen peripheral boron atoms and sixteen interior atoms. There is an out-of-plane distortion of 1.54 Å. Interestingly, the global minimum isomer **V** of B_{34}^- with C_1 symmetry is chiral due to the nonplanarity and the position of the hexagonal vacancy. Its degenerate enantiomer is shown in Figure 3b as isomer **VI** (C_1 , ²A). In fact, the chiral B_{34}^- global minimum is related to the chiral B_{30}^- cluster reported previously by adding four more boron atoms along one edge.^[39]

The low-lying isomers of B_{34}^- are also mainly of 2D structures with polygonal vacancies (Figure S2). Within 1 eV of the global minimum, only two 3D structures are found among the 29 lowlying isomers, i.e., a cage-like isomer (**VII** in Figure 3b) and a double-ring tubular isomer (C_{2h} , 2A_g). These 3D isomers are 0.26 and 0.51 eV above the global minimum, respectively. The fourth isomer (**VIII** in Figure 3b) is 2D with a hexagonal vacancy next to a filled pentagonal site.

Neutral B₃₃ and B₃₄ Clusters

On the bases of the anion isomers, we optimized the same sets of structures for neutral B_{33} and B_{34} at the PBE0/6-311+G(d) level. The top four isomers for each cluster are presented in Figure S3 (**I'–VIII'**), which correspond to the top four isomers of the respective anions, but with slight different energetic ordering. Notably, the 3D cage-like isomer **V**' for B_{34} is overwhelmingly more stable than the 2D isomers. This change of energetic orders between neutral and anionic species has been observed previously for a number of even-sized boron clusters, in particular in $B_{28}^{-/0}$ and $B_{40}^{-/0}$.^[37,52] This reversal is usually associated

with a large HOMO–LUMO gap in the 3D cage isomers, which makes the cage isomers energetically less favorable in the anion because the extra electron occupies a higher energy LUMO.

Discussion

Comparison between Experiment and Theory

We calculated the VDEs for the top four lowest-lying isomers of B_{33}^- (I–IV) and B_{34}^- (V–VIII) using the time-dependent DFT (TD-DFT) method at the TD-PBE0/6-311+G(d) level.^[60] Simulated PE spectra for the global minima of B_{33}^- and B_{34}^- are compared with the experimental spectra in Figure 1 and Figure 2, respectively. Those for the low-lying isomers for the two clusters are shown in Figures S4 and S5, respectively.

B₃₃⁻

The low-lying isomers of B_{33}^{-} are all closed-shell, resulting in doublet final states upon one-electron detachment. As shown in Table S1, removals of an electron from the HOMO (23a'') and HOMO-1 (27a') of isomer I yield similar VDEs, 4.03 vs. 4.09 eV, which are in good agreement with band X in the experimental spectrum at 4.09 eV (Figure 1a). The calculated ADE of 3.92 eV also agrees well with the experimental value (3.91 ± 0.04 eV). The third detachment channel is from the 26a' orbital with a computed VDE of 4.57 eV, in good agreement with the relatively well-resolved band A at 4.62 eV. The next five detachment channels give rise to closely spaced VDEs, consistent with the congested spectral features from B to E in the higher binding energy range (Figure 1a). Overall, the simulated PES pattern of isomer I is in excellent agreement with the experiment, strongly confirming the identified global minimum.

The calculated first VDEs for isomers **II**, **III**, and **IV**, are 3.55, 3.67, and 3.79 eV, respectively, which deviate substantially from the experimental value (4.09 eV). Furthermore, their simulated PES patterns (Figure S4) do not agree with the experimental spectrum. Thus, these isomers are unlikely to be populated in the cluster beam.

B₃₄⁻

Because the global minimum isomer **V** (C_1 , ²A) for B_{34}^- is openshell, both singlet and triplet final states are possible upon oneelectron detachment, resulting in a more complicated PE spectrum. The computed first ADE and VDE for the global minimum V are 3.74 and 3.84 eV, respectively, in good agreement with the experimental values of 3.75 and 3.89 eV, respectively, from band X, due to electron detachment from the SOMO (52a). As shown in Table S1, the next four detachment channels are derived from electron detachment from the fully occupied 51a and 50a orbitals. The computed VDEs of these detachment channels are closely spaced (from 3.96 eV to 4.38 eV) and are also close to the first detachment channel. The congested first five detachment channels are in good agreement with the observed bands in the lower binding energy region (bands X, A, B). The next detachment channel from the 49a orbital yields a computed VDE of 5.07 eV (Table S1), well separated from the first five detachment channels. The theoretical data revealed

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ten detachment channels from 5.07 to 6.23 eV, in good agreement with the congested spectrum in the higher binding energy region.

Since isomer **VI** is the enantiomer of isomer **V**, it yields the same simulated PE spectrum, as shown in Figure S5b. The simulated spectra of isomers **VII** and **VIII** do not agree with the experiment (Figure S5). Overall, the excellent agreement between the simulated spectra of isomers **V/VI** and the experimental spectrum lends considerable credence for the identified chiral global minimum for B_{34}^{-} .

Bonding Analysis

We analyzed the chemical bonding of the global minima of B_{33}^- (**I** C_s , ¹A') and B_{34}^- (**V** C_1 , ²A) using the adaptive natural density partitioning (AdNDP) approach.^[61] The bonding analyses were done using the planarized species, i.e., a $C_{2\nu} B_{33}^-$ and a closed-shell $C_s B_{34}^{2-}$ for better visualization of the σ vs. π bonds, as shown in Figure 4a and Figure 5, respectively. We used the closed shell B_{34}^{2-} , instead of the open-shell B_{34}^- for the convenience of the bonding analyses.^[61] We also analyzed the bonding for the closed-shell B_{34} (see Figure S6).



Figure 4. Results of the AdNDP analyses for (a) $C_{2\nu} B_{33}^{-}$ and (b) $C_{2\nu} C_{19} H_{11}^{-}$.

Among the 100 valence electrons in B_{33}^- , the AdNDP analysis recovered eighteen localized peripheral 2c–2e σ B–B bonds, six 3c–2e bonds around the central hexagon, and sixteen 4c–2e bonds between the inner hexagon and the cluster periphery (Figure 4a). The remaining valence electrons form ten delocalized π bonds. Interestingly, the π bonding in the 2D B_{33}^- is similar to that in the polycyclic aromatic hydrocarbon $C_{19}H_{11}^-$





Figure 5. Results of the AdNDP analysis for the closed-shell $C_s B_{34}^{2-}$.

(Figure 4b), suggesting the aromatic character of the boron cluster. Thus, the 2D B_{33}^- cluster can be considered as a new example of all-boron analogues of hydrocarbons.^[17,23-29,32,39-42]

The σ bonding in B₃₄^{2–} (Figure 5) is almost identical to that in B₃₃⁻. Among the 104 valence electrons, there are eighteen peripheral 2c–2e σ B–B bonds, six 3c–2e bonds around the central hexagon, and sixteen 4c-2e bonds between the inner hexagon and the cluster periphery. However, the π bonding in the 2D B₃₄²⁻ species is slightly different and can be seen to consist of two delocalized π systems, including nine 5c-2e π bonds around the periphery and three 5c–2e π bonds around the inner hexagon. Each π system obeys the 4N+2 Hückel rule for aromaticity. This observation suggests that the 2D B₃₄²⁻ cluster can be considered to be doubly π -aromatic. The bonding in the 2D neutral B_{34} (Figure S6) is identical to that in the 2D B_{34}^{2-} , except that there are only two 5c–2e π bonds around the inner hexagon, making this π system antiaromatic. The latter may underlie the reason why the 2D B₃₄ neutral is less stable than the 3D isomer (Figure S3).

Structural Evolution in Mid-Sized Boron Clusters

It should be noted that the hexagonal vacancy, essential for the stability of borophenes,^[41] is the most important structural feature in mid-sized boron clusters, starting from $B_{26}^{-.[35]}$ The role of the hexagonal vacancy in the stability of B_{36} has been further analyzed recently.^[62] The hexagonal vacancy in the global minima of B_{33}^{-} and B_{34}^{-} implies that B_{35}^{-} is the smallest cluster to possess a double-hexagonal vacancy.^[40] It is interesting to see the evolution of the double-hexagonal vacancy among the low-lying isomers in B_{33}^{-} and B_{34}^{-} . In B_{33}^{-} (Figure S1), the first isomer with a double-hexagonal vacancy is 0.9 eV above the global minimum, whereas in B_{34}^{-} (Figure S2) the first isomer with a double-hexagonal vacancy is only 0.42 eV above the global minimum. The isomer with a double-hexagonal vacancy seems to gain stability from B_{33}^- to B_{35}^- , where it becomes the global minimum. It should be noted that among the low-lying isomers of B₃₄⁻ there appears an isomer with a triplehexagonal vacancy being 0.87 eV above the global minimum. Such structural features are reminiscent of those in the χ_3 borophene,^[63] consisting of roles of hexagonal vacancies.





Conclusions

We have studied the structures and chemical bonding of the B_{33}^- and B_{34}^- clusters using photoelectron spectroscopy and DFT calculations. Global minimum searches in conjunction with the experiment show that the most stable structures of both B_{33}^- and B_{34}^- are 2D with a central hexagonal vacancy. The global minimum of B_{33}^- has C_s symmetry, whereas that of B_{34}^- is chiral with C_1 symmetry. Chemical bonding analyses reveal that the 2D B_{33}^- and B_{34}^- are aromatic with the π bonding in B_{33}^- being analogous to that in the $C_{19}H_{11}^-$ polycyclic aromatic hydrocarbon. The current study confirms that the B_{35}^- cluster is the smallest boron cluster to feature a double-hexagonal vacancy.

Methods

Photoelectron Spectroscopy: The experiments were carried out using a magnetic-bottle PES apparatus equipped with a laser vaporization supersonic cluster source, details of which can be found elsewhere.^[17,54] Boron clusters were produced by laser vaporization of a hot-pressed ¹⁰B-enriched disk target. Clusters formed in the nozzle were entrained by a He carrier gas seeded with 5 % Ar and underwent a supersonic expansion. Negatively charged clusters were extracted from the collimated cluster beam after a skimmer and analyzed using time-of-flight mass spectrometry. The B₃₃⁻ and B₃₄⁻ clusters of interest were mass-selected and decelerated before being intercepted by a detachment laser beam. Owing to the relatively high binding energies of B_{33}^- and B_{34}^- , the 193 nm (6.424 eV) radiation from an ArF excimer laser was used to conduct the experiment. Photoelectrons were collected at nearly 100 % efficiency using a magnetic bottle and analyzed in a 3.5 m long electron flight tube. The PE spectra were calibrated using the known spectrum of Au⁻. The energy resolution of the instrument was $\Delta E_k/E_k \approx 2.5$ %, that is, ≈ 25 meV for 1 eV kinetic energy electrons.

Computational Methods

We conducted global minimum searches for B_{33}^- and B_{34}^- using an improved basin-hopping (BH) algorithm implemented in the TGMin code,^[55,56] which has proved to be effective for B_n^- (n = 30, 35– 38) clusters.^[39–42] Structural searches for the closed-shell B_{33}^- were straightforward, but for the open-shell B_{34}^- we first did the structural search using the closed-shell $B_{34}^-^2$ species to save computational time. Subsequently, low-lying isomers of B_{34}^{-2} were detached by one electron to achieve the B_{34}^- isomers with further structural optimization. For each anion cluster, four different 2D structures and one random 3D isomer were used as seed structures to run the BH searches. A total of 2760 and 2721 stationary points were probed for B_{33}^- and B_{34}^{2-} , respectively. In addition, manual structural constructions were also used to aid the searches for the typical 3D double/triple-ring tubular structures and facile 2D structures based on 2D B_n^- (n = 26-30, 35–38) clusters.^[35–42]

The obtained low-lying isomers of B_{33}^- and B_{34}^- were re-optimized at the PBE0/6-311+G(d) level.^[57–59] Vibrational frequencies were calculated at the same level to ensure that the reported structures are true minima on the potential energy surfaces. For comparison with experimental data, VDEs and ADEs were computed for low-lying isomers of B_{33}^- and B_{34}^- at the TD-PBE0/6-311+G(d) level.^[60] PBE0 and TD-PBE0 calculations were done using the Gaussian 09 package.^[64] Bonding analyses were performed using the AdNDP method^[61] and visualized via Molekel 5.4.0.8.^[65]

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